

Review.

1. Simplify as much as possible:  $\sin^2(x) + \cos^2(x)$ .

2. Write in terms of only  $\sin(x)$  and  $\cos(x)$ :

$\tan(x) \qquad \cot(x)$

$\sec(x) \qquad \csc(x)$

3. Expand using angle sum formulas:

$\sin(x + h) \qquad \cos(x + h)$

4.  $\lim_{h \rightarrow 0} \frac{\sin h}{h}$

5. (review-ish)  $\lim_{h \rightarrow 0} \frac{\cos(h) - 1}{h}$

Problems.

1. Use the definition of the derivative to prove that  $\frac{d}{dx}(\sin(x)) = \cos(x)$ .

2. Use the differentiation formulas for  $\sin(x)$  and/or  $\cos(x)$  to verify the differentiation rule for  $\tan(x)$ .

3. Determine  $\frac{d}{dx} \left( \frac{1}{\sqrt{x}} + \sin(x) \right)$ .

4. Determine  $f''(x)$  for  $f(x) = 14 \sec x$ .

5. Differentiate the following functions.

(a)  $f(x) = \frac{19}{\sin(x)}$

(b)  $y = \sqrt{x} \tan(x) + \cos(x)$

(c)  $y = x^2 \cos(x) - 3x \sin(x)$

(d)  $f(x) = \frac{\sin(x)}{2 + \tan(x)}$

(e)  $f(x) = \frac{e^x \sin(x) - 1}{x + 3}$

(f)  $y = (x + e^x) \left( \frac{\sin(x)}{\cot(x) + 12} \right)$

6. Determine an equation of the tangent line to the graph of  $y = \cot(x)$  when  $x = \pi/4$ .

7. Use the differentiation formulas for  $\sin(x)$  and/or  $\cos(x)$  to verify the differentiation rule for  $\csc(x)$ .

8. Use the definition of the derivative to prove that  $\frac{d}{dx}(\cos(x)) = -\sin(x)$ .